



Cambridge International AS & A Level

CANDIDATE
NAME

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CENTRE
NUMBER

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FURTHER MATHEMATICS

9231/02

Paper 2 Further Pure Mathematics 2

For examination from 2020

SPECIMEN PAPER

2 hours

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [].

This document has **18** pages. Blank pages are indicated.

2 Find the exact value of $\int_0^1 \frac{1}{\sqrt{3+4x-4x^2}} dx$.

[6]

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3 Find the solution of the differential equation

$$x \frac{dy}{dx} + 3y = \frac{\sin x}{x}$$

for which $y = 0$ when $x = \frac{1}{2}\pi$. Give your answer in the form $y = f(x)$.

[8]

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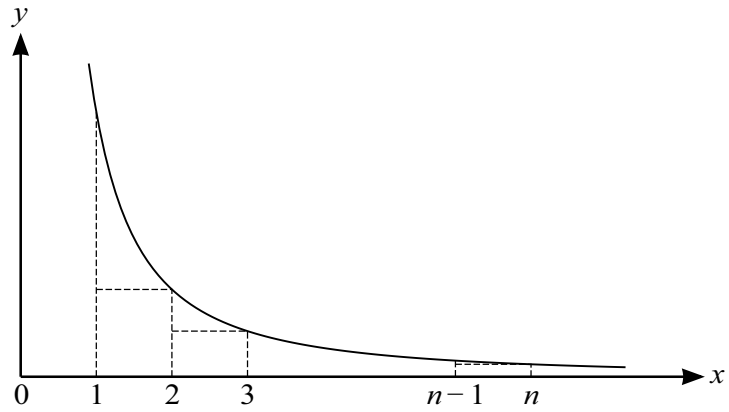
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4



The diagram shows the curve with equation $y = \frac{1}{x^2}$ for $x > 0$, together with a set of $(n-1)$ rectangles of unit width.

(a) By considering the sum of the areas of these rectangles, show that

$$\sum_{r=1}^n \frac{1}{r^2} < \frac{2n-1}{n}. \quad [5]$$

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- (b) Use a similar method to find, in terms of n , a lower bound for $\sum_{r=1}^n \frac{1}{r^2}$. [3]

